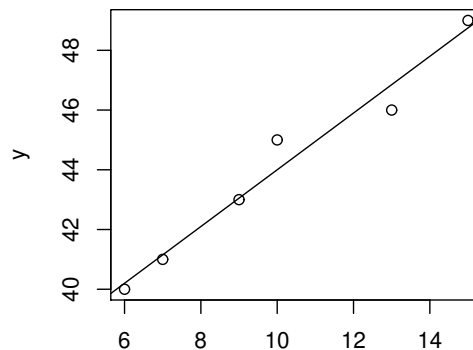


HOMEWORK: CORRELATION, SIMPLE REGRESSION
ELEMENTARY STATISTICS AND INFERENCE (STAT:1020; BOGNAR)

1. At a large company, the salaries (y , in thousands of dollars) and years of experience (x) of six randomly chosen engineers are

$x = \text{years:}$	6	7	9	10	13	15
$y = \text{salary:}$	40	41	43	45	46	49

- (a) Find Pearson's sample correlation coefficient r .
 $Cov(x, y) = 11.4$, $s_x = 3.464$, $s_y = 3.347$, $r = 0.983$.
- (b) Determine the least squares regression line.
 $\hat{y} = 34.5 + 0.95x$
- (c) Carefully make a scatter-plot of the dataset and draw the regression line (place the explanatory variable x on the horizontal axis, and the response variable y on the vertical axis).



- (d) On average, each extra year of experience yields how much extra pay?
 $0.95 = \$950$
- (e) What is the approximate average starting pay?
 $34.5 = \$34500$
- (f) Approximate the mean salary for engineers with 6 years of experience, i.e. approximate $\mu_{y|x=6}$.
 $\hat{y} = 34.5 + 0.95(6) = 40.2 = \40200
- (g) Find a 95% confidence interval for the population mean salary for engineers with 6 years of experience, i.e. find a 95% CI for $\mu_{y|x=6}$. Interpret the CI. *Hint: According to Minitab, $\widehat{se}(\hat{y}) = 0.448$.*
 $\hat{y} \pm t_{\alpha/2, n-p} \widehat{se}(\hat{y}) = 40.2 \pm 2.776(0.448) = (38.96, 41.44)$
- (h) Is there a significant linear relationship between years of experience and salary? *Hint: According to Minitab, $\widehat{se}(\hat{\beta}_1) = 0.0878$. You must state H_0 and H_a (use $\alpha = 0.05$), find the test statistic and critical value, plot the rejection region, and state your decision and final conclusion.*
 $H_0 : \beta_1 = 0$, $H_a : \beta_1 \neq 0$, $t^* = (\hat{\beta}_1 - \beta_1) / \widehat{se}(\hat{\beta}_1) = 10.82$, $t_{\alpha/2, n-p} = 2.776$, reject H_0 , evidence that $\beta_1 \neq 0$, significant linear relationship between years of experience and salary.
- (i) Approximate the p -value for the test in (1h). Based upon your p -value, is there a significant linear relationship between years of experience and salary? Why?
 $p\text{-value} = 2P(t_{(4)} > 10.82) < 0.001$, significant linear relationship between years of experience and salary since $p\text{-value} < \alpha$
- (j) Find a 95% confidence interval for β_1 . Based upon your CI, is there a significant linear relationship between years of experience and salary? Why? *Hint: According to Minitab, $\widehat{se}(\hat{\beta}_1) = 0.0878$.*
 $\hat{\beta}_1 \pm t_{\alpha/2, n-p} \widehat{se}(\hat{\beta}_1) = 0.95 \pm 2.776(0.0878) = (0.706, 1.194)$, significant linear relationship since CI excludes 0
- (k) Find a 95% confidence interval for the (population) mean starting salary, i.e. find a 95% CI for $\beta_0 = \mu_{y|x=0}$.
Hint: According to Minitab, $\widehat{se}(\hat{\beta}_0) = 0.9208$.
 $\hat{\beta}_0 \pm t_{\alpha/2, n-p} \widehat{se}(\hat{\beta}_0) = 34.5 \pm 2.776(0.9208) = (31.94, 37.06)$
- (l) In reference to question (1k), is the population mean starting salary significantly different than 40 (i.e. \$40,000)? Why?
 Yes, since the CI excludes 40