

22S:138

Lab session 1

Using R functions for simple Bayesian analysis

Aug. 29, 2008

1 Getting started

Log onto the lab computers using your HawkID and password. If you do not know these, you can use the temporary password for the day.

2 The course home page

Bring up Internet Explorer. Type in the URL (address) of the course homepage:

www.stat.uiowa.edu/~kcowles/s138_2008

Look at the sections entitled "Handouts," "Datasets," and "Web resources."

We will download two files from the "Handouts" section. Right-click on the file name `bayes`; then choose "Save target as." Save the file on the Desktop if you want to use it only during this lab. If you wish to access the file later without having to download it again, save it to your own H: directory or to a flash drive.

Right-click and save `plot.beta` as well.

Notice whether the files are saved with or without a filename extension of `.txt` or `.htm`. Different web browsers will do this differently. You can right-click on the icon of the saved file, and then click "Properties" to see the full path name of the saved file.

3 Using my R functions

I have written some functions to make some simple Bayesian calculations and graphics easy. Those of you who know R or Splus are welcome to write and use better functions of your own, but mine are adequate for the assigned work at the beginning of the semester. They are based on the Minitab and Matlab macros by Jim Albert. Later in the semester we will use R libraries written by others, as well as the software package WinBUGS, to fit more complicated models.

Bring up R from the All Programs menu.

You will need to use the "source" command to install each of my functions in your R work area before using it.

To install my function to do simple sequential Bayesian analysis with Bayes theorem, and to give it the name "s138.bayes," enter the following command (this assumes you saved into the Documents folder on the desktop; substitute your user name for `kcowles`):

```
s138.bayes <- source("C:\\users\\kcowles\\Documents\\bayes.txt")$value
```

If you used a web browser that did not automatically add the extension `.txt` to the filename, or added a different extension, you will instead have to modify the filename accordingly when you read the function into R.

If you have access to S-Plus and are using it instead of R for your homework, you will not have to put the "\$value" on the end of the "source" command.

To run an R function, enter its name, followed by parentheses.

```
> s138.bayes()
```

Try using this function to work the problem we did in lecture with a student's disease status and the screening test. The prompts, and your appropriate responses are as follows:

Input number of models, followed by return key

(Leave blank and hit return to exit):

(Leave blank and hit return to exit):

1: 2

2:

Input names of models, one on each line:

1: disease

2: no disease

3:

Input prior probabilities of models, one on each line:

1: .001

2: .999

3:

Input number of possible outcomes, followed by return key:

1: 2

2:

Input the name of each possible outcome, one on each line:

1: +

2: -

3:

```
[1] "2"          "disease"     "no disease"  "0.001"      "0.999"
```

Input the likelihood of each possible outcome under each model:

Model 1 :

1: .95

2: .05

3:

Model 2 :

1: .05

2: .95

3:

```
[1] 2 2
```

Table of priors and likelihoods

1	disease	0.001	0.95	0.05
---	---------	-------	------	------

2	no disease	0.999	0.05	0.95
---	------------	-------	------	------

Input number of observations, followed by return key:
 1: 3
 2:
 Input the names of the observations, one on each line:
 1: +
 2: +
 3: -
 4:

The function produces the following output:

```

Observation: +
Update Based on Bayes' Theorem
      Models  Prior  Like    Prod    Post
[1,] "disease"  "0.001" "0.95" "0.00095" "0.01866"
[2,] "no disease" "0.999" "0.05" "0.04995" "0.98134"

```

```

Observation: +
Update Based on Bayes' Theorem
      Models  Prior  Like    Prod    Post
[1,] "disease"  "0.01866" "0.95" "0.01773" "0.2654"
[2,] "no disease" "0.98134" "0.05" "0.04907" "0.7346"

```

```

Observation: -
Update Based on Bayes' Theorem
      Models  Prior  Like    Prod    Post
[1,] "disease"  "0.2654" "0.05" "0.01327" "0.01866"
[2,] "no disease" "0.7346" "0.95" "0.69787" "0.98134"

```

Notice that at each step, the “posterior” from the previous step becomes the new “prior.”

4 An example with 3 possible models and 5 possible outcomes

The book *Bayesian Computation Using Minitab* by Jim Albert, Wadsworth Publishers, 1996, describes a sequential Bayesian analysis using generalized Bayes’ theorem.

Here is an excerpt from the book:

...suppose that a new student is attending a high school, and the principal is uncertain about the student’s ability. This administrator classifies students as either “good,” “mediocre,” or “poor.” (These three types of students will represent the *models* in this problem.) The principal knows very little about this particular student, but she is familiar with other students who have transferred in from the same community. Of these transfer students, she believes that 60% were good, 30% were mediocre,

and only 10% were poor. The administrator thinks that the new student is representative of other students that have come from this community, and so she believes that the student is good, mediocre, or poor with respective probabilities .6, .3, and .1.

The principal is also knowledgeable about the types of grades in core subjects earned by students of the three types. In these courses, the possible grades are A, B, C, D, and F. For each course, suppose that a “good student” gets either an A, B or C with probabilities .4, .4, .2, respectively. A “mediocre student” gets A, B, C, D, or F, with respective probabilities .1, .2, .4, .2, .1, and a “poor students” will only get a C, D, or F, with probabilities .3, .5, .2. ... the *data* refers to a particular grade in a course. There are five possible *observations*, and the *likelihoods* are the given probabilities of the five different grades for the three different types of student.

The principal will learn more about the ability of the student after he has taken some classes. Suppose that he takes four classes and the grades in the four courses are independent (which means that the student’s chances of a particular grade in one course are not dependent on his performance in other courses). At the end of the term, the principal observes that the student gets two B’s and two C’s. What does the principal now think about the student’s ability?

The R function may be used to carry out this example as follows:

```

> s138.bayes()
Input number of models, followed by return key
(Leave blank and hit return to exit):
1: 3
2:
Input names of models, one on each line:
1: good
2: mediocre
3: poor
4:
Input prior probabilities of models, one on each line:
1: .6
2: .3
3: .1
4:
Input number of possible outcomes, followed by return key:
1: 5
2:
Input the name of each possible outcome, one on each line:
1: A
2: B
3: C
4: D
5: F

```

```
6:
[1] "3"      "good"    "mediocre" "poor"    "0.6"     "0.3"     "0.1"
```

Input the likelihood of each possible outcome under each model:

Model 1 :

```
1: .4
2: .4
3: .2
4: 0
5: 0
6:
```

Model 2 :

```
1: .1
2: .2
3: .4
4: .2
5: .1
6:
```

Model 3 :

```
1: 0
2: 0
3: .3
4: .5
5: .2
6:
```

```
[1] 3 5
```

Table of priors and likelihoods

	good	mediocre	poor
1	0.6	0.3	0.1
2	0.4	0.2	0.0
3	0.4	0.4	0.3
4	0.2	0.4	0.5
5	0.2	0.2	0.2

Input number of observations, followed by return key:

```
1: 4
2:
```

Input the names of the observations, one on each line:

```
1: B
2: B
3: C
4: C
5:
```

Observation: B

Update Based on Bayes' Theorem

	Models	Prior	Like	Prod	Post
[1,]	"good"	"0.6"	"0.4"	"0.24"	"0.8"
[2,]	"mediocre"	"0.3"	"0.2"	"0.06"	"0.2"
[3,]	"poor"	"0.1"	"0"	"0"	"0"

Observation: B

Update Based on Bayes' Theorem

	Models	Prior	Like	Prod	Post
[1,]	"good"	"0.8"	"0.4"	"0.32"	"0.88889"
[2,]	"mediocre"	"0.2"	"0.2"	"0.04"	"0.11111"
[3,]	"poor"	"0"	"0"	"0"	"0"

Observation: C

Update Based on Bayes' Theorem

	Models	Prior	Like	Prod	Post
[1,]	"good"	"0.88889"	"0.2"	"0.17778"	"0.8"
[2,]	"mediocre"	"0.11111"	"0.4"	"0.04444"	"0.2"
[3,]	"poor"	"0"	"0.3"	"0"	"0"

Observation: C

Update Based on Bayes' Theorem

	Models	Prior	Like	Prod	Post
[1,]	"good"	"0.8"	"0.2"	"0.16"	"0.66667"
[2,]	"mediocre"	"0.2"	"0.4"	"0.08"	"0.33333"
[3,]	"poor"	"0"	"0.3"	"0"	"0"

After the student receives his first grade (B), what is the principal's posterior probability that the student is a mediocre student?

5 Printing the output from an R function

Probably the easiest way to print R output is to copy it into Notepad or Wordpad and edit and print it from there.

6 R graphics

You won't need this for the first homework, but you will for next week's homework.

Obtain my function for plotting beta densities:

```
> s138.plot.beta <- source("c:\\temp\\plot.beta.txt")$value
```

Then run it.

```
> s138.plot.beta()
```

We'll learn about the beta density next week. For right now, you just need to remember that each of the two parameters must be greater than 0.

Input alpha and beta parameters for the beta density, on separate lines, followed by return key :

```
1: 3.4
2: 29.1
```

3:

To remove the graphics window, enter

```
dev.off()  
at the prompt.
```

A new window should appear, containing a plot. In the upper border of the plot, R will tell you the “device number” of the plot, and whether or not this is the “active” device. To print the plot in the active device, enter

```
dev.print(device=win.print)
```

If you ran this function many times, you would get a new graphics window every time. If you wish to print a plot *other* than the active one, you can make a different device active. For example, to make device 2 the active device and then print the plot in device 2, enter

```
dev.set(2)  
dev.print(device=win.print)
```

To close an active graphics window, enter

```
dev.off()
```

It is also possible to copy an R graph into a Word document. Right click on the plot window; then select “Copy as bitmap.” Then paste into an open Word document.

7 Ending a session

R maintains what it calls the “workspace,” in which it stores any function or other objects that have created during a given session. If you exit from R without saving the workspace image, then any new objects you have created during the session will be lost. If you are working on a lab computer and wish to save your work to a flash drive so that you can reload it into R on another computer later, use the “File” menu to *change the working directory* to the appropriate drive now.

To exit from R enter

```
> q()
```

You will be asked whether you want to save the workspace image. If you respond “No,” then any new work done during this session will be lost. If you are working on your own computer, and you want these functions to remain associated with R so you don’t have to “source” them in again next time, choose “Yes.” If you are working on a lab computer and have previously changed the working directory to a flash drive or to your H: drive, then the workspace image will be saved there.

Be sure to log off the computer (using the All Programs menu) before you leave.

To access a saved workspace next time you use R:

1. start R
2. use the File menu to :
 - (a) Change dir

(b) Load workspace